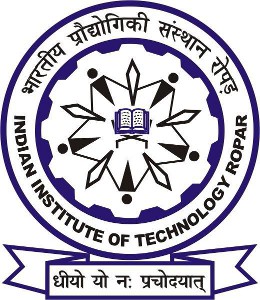
horizontal line

**EE208:CONTROL ENGINEERING LAB 09**

**Simulation and control design on Simulink as a CAD interface to MATLAB**

**Course Instructor : Dr. Sanjay Roy**

**Date : 21th March 2022**



**Group Number - 14**

**Raj Kumar Deb 2020eeb1025**

**Tushar Sharma 2020eeb1325**

**Tiya Jain 2020eeb1213**

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# 1. OBJECTIVE

Analyse the effectiveness of Ziegler-Nichols rules in presence of poles with high multiplicity.

(as a CAD interface to MATLAB)

# 2. GIVEN INFORMATION

The basic OLTF unit provided that is to be considered at different multiplicities :

In the above equation, assumes any integer value between one to ten .

# 3. INTRODUCTION : Ziegler-Nichols Rules

The intention of Ziegler-Nichols tuning rules was to achieve a fast closed loop step response without excessive oscillations and excellent disturbance rejection. Ziegler and Nicholas proposed some rules for determining the values of

a) - Controller’s path gain

b) - Controller’s integrator time constant

c) - Controller’s derivative time constant .

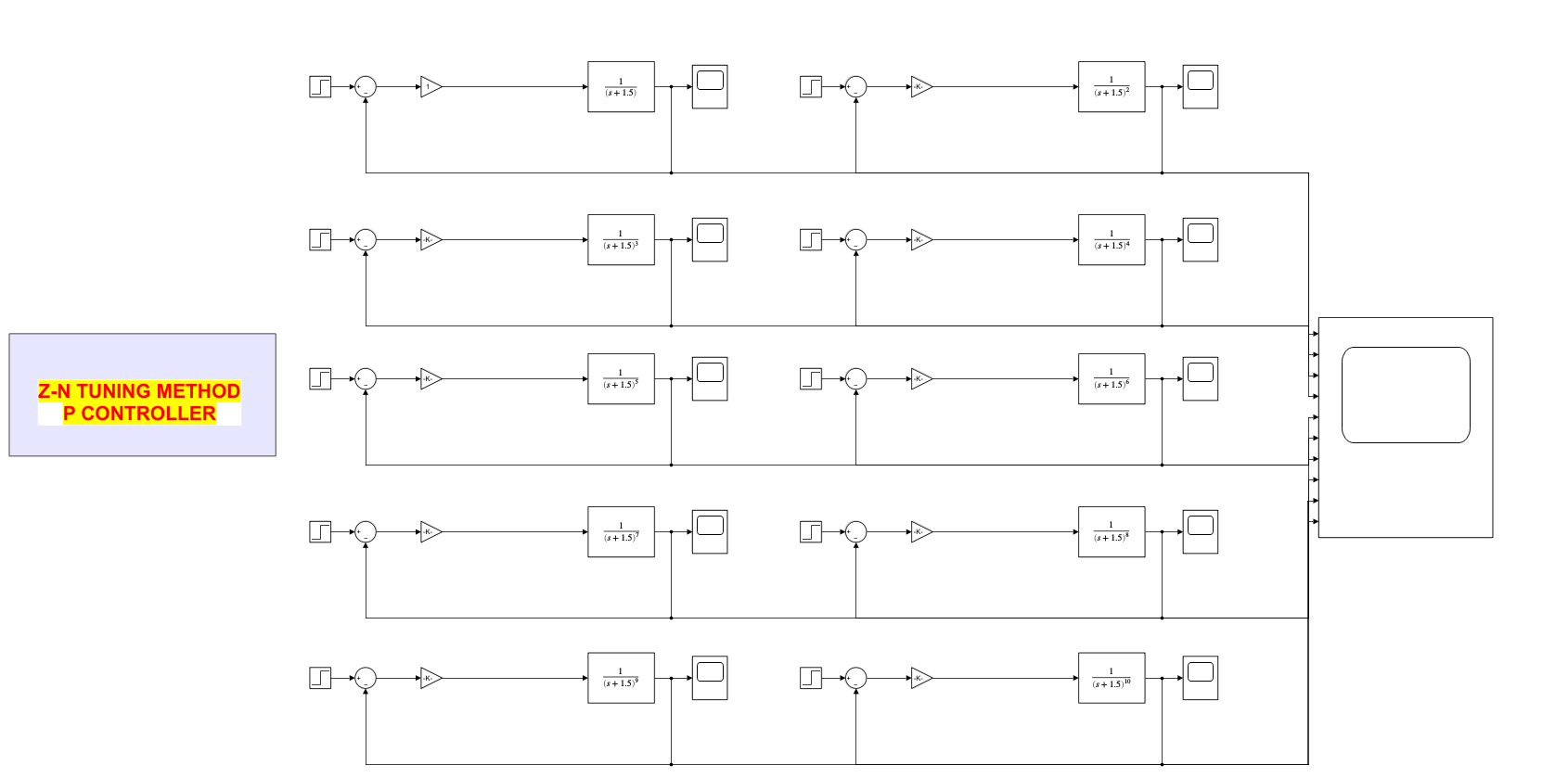
The two methods of the Ziegler-Nichols tuning are described below:

| **First Method : LAG TYPE RESPONSE** | **Second method : OSCILLATORY TYPE RESPONSE** |
| --- | --- |
| Based on open-loop concepts relying on reaction curves | Based on closed-loop concepts requiring the computation of the critical gain and critical period |
| Obtain experimentally the response of the plant to a unit-step input. | Set |
| The process gain is defined as where Y SS is the steady state value of the output response. Thus, gain parameter | If the output does not exhibit sustained oscillations for whatever value Kp may take, then this method does not apply. |
| | **Type** |  |  |  | | --- | --- | --- | --- | | **P** |  |  | 0 | | **PI** |  |  | 0 | | **PID** |  |  |  | | | **Type** |  |  |  | | --- | --- | --- | --- | | **P** |  |  | 0 | | **PI** |  |  | 0 | | **PID** |  |  |  | |

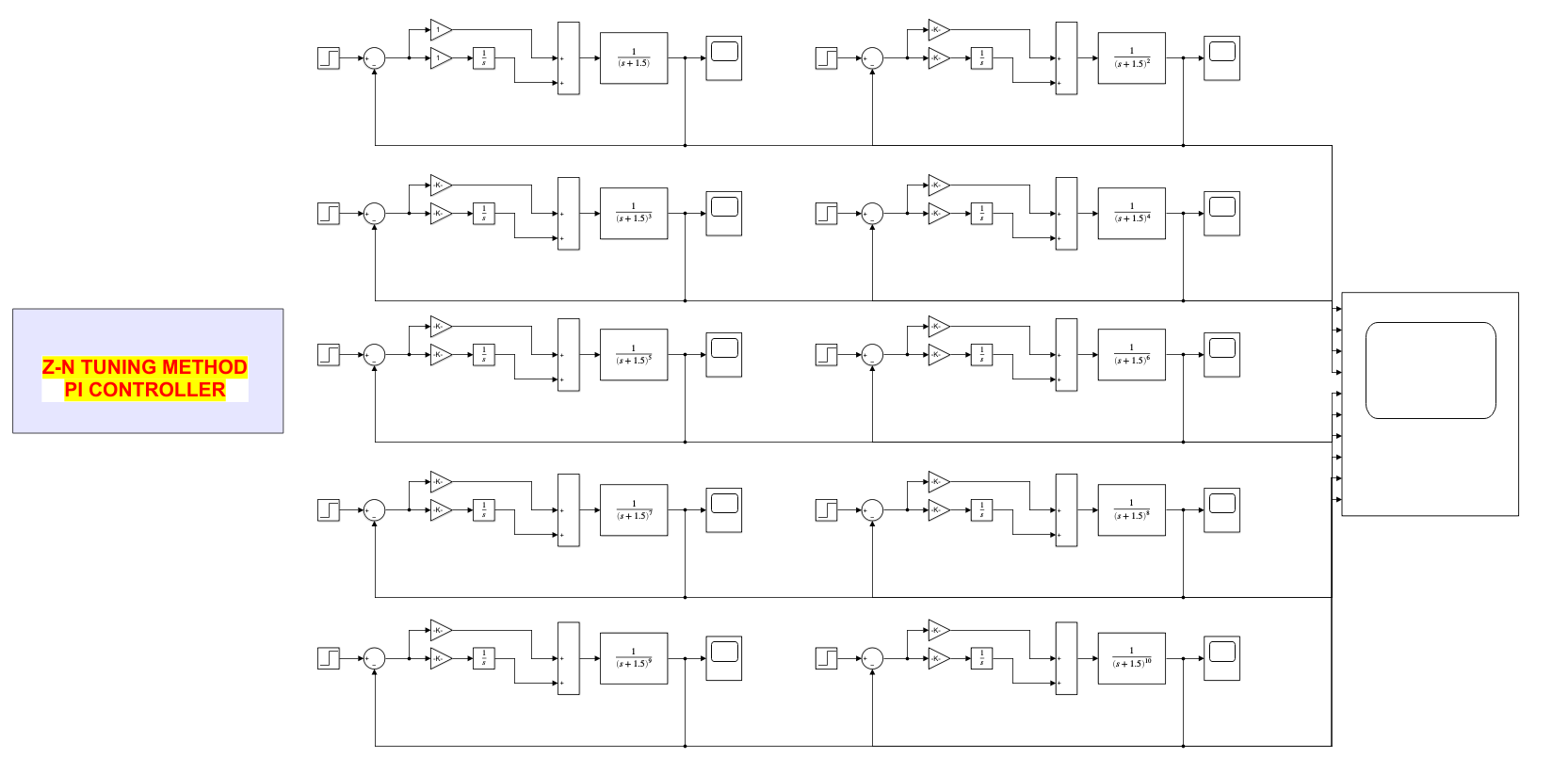
# 4. ZIEGLER - NICHOLS TUNING METHOD

## 4.1. Simulink Diagrams

### 4.1.1 P controller for **)**

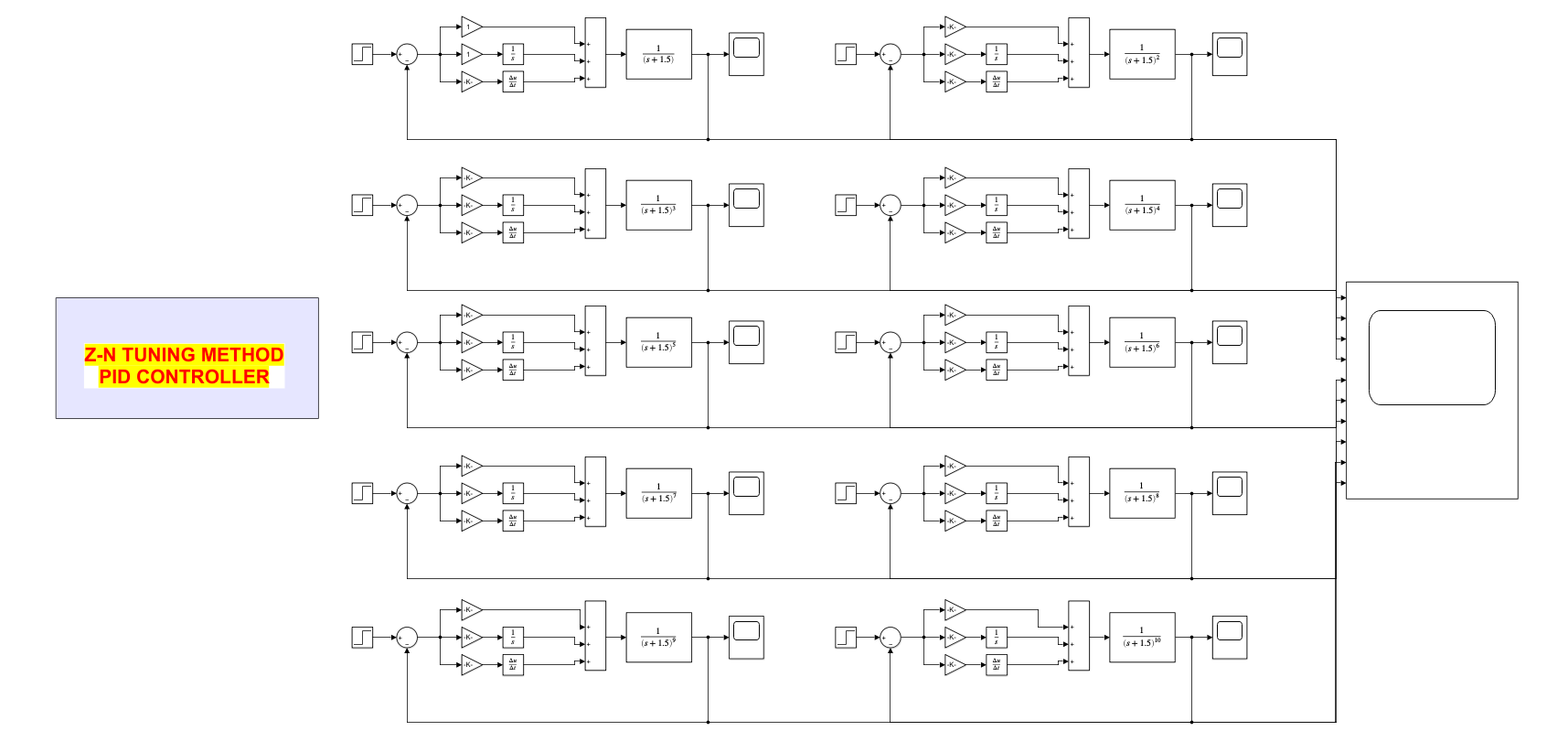
****

### 4.1.2 PI controller for **)**

****

### 

### 4.1.3 PID controller for **)**

****

## 4.2. Tuned constants for P, PI, and PID control

### 4.2.1 P controller for **)**

| Constants | n=1 | n=2 | n=3 | n=4 | n=5 | n=6 | n=7 | n=8 | n=9 | n=10 |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | - | 9.6295 | 4.5867 | 3.1305 | 2.4336 | 2.0236 | 1.7503 | 1.5563 | 1.4097 | 1.2927 |
|  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
|  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

### 4.2.2 PI controller for **)**

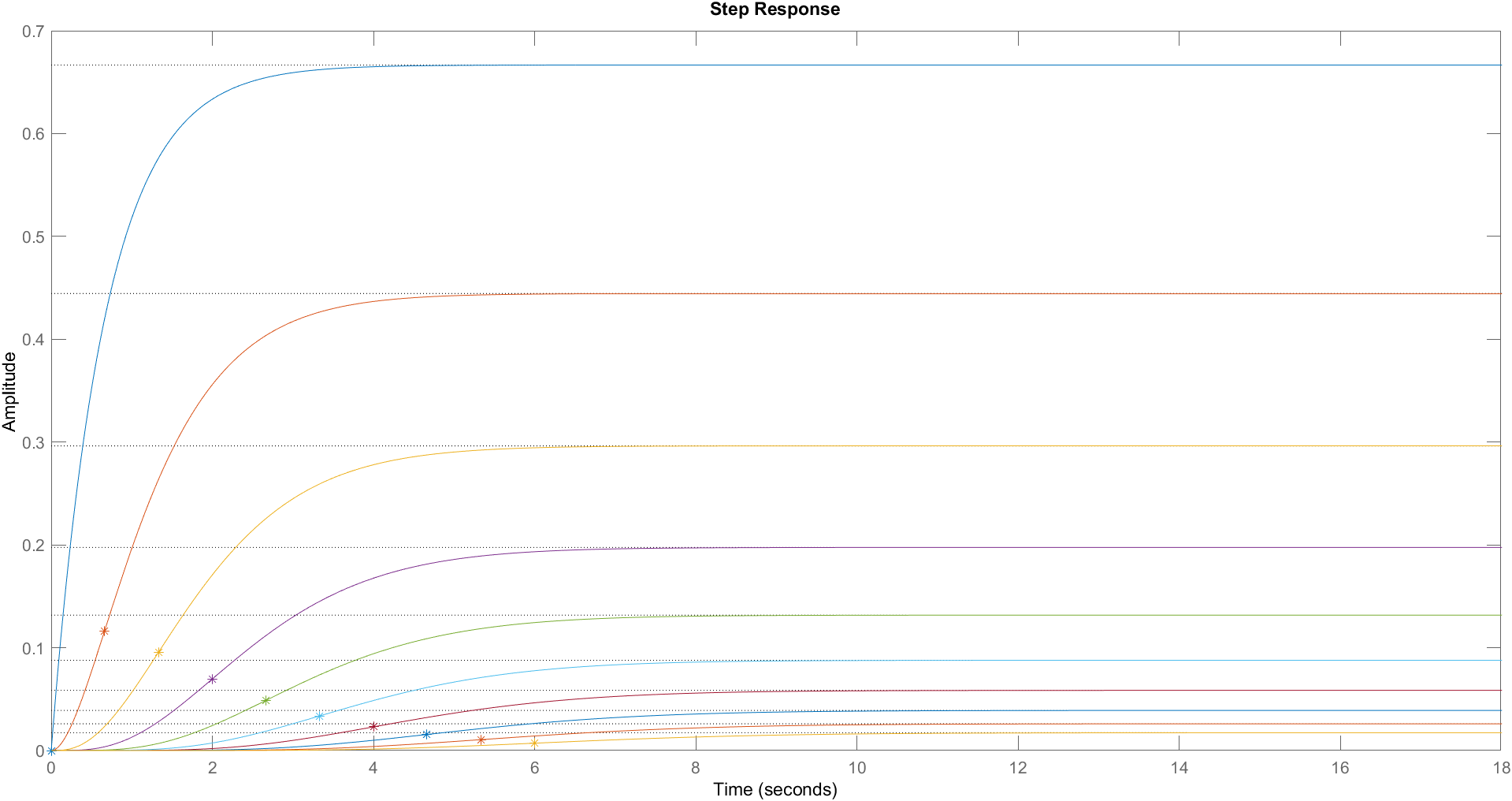
| Constants | n=1 | n=2 | n=3 | n=4 | n=5 | n=6 | n=7 | n=8 | n=9 | n=10 |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | Inf | 8.6666 | 4.1280 | 2.8175 | 2.1903 | 1.8213 | 1.5753 | 1.4007 | 1.2688 | 1.1635 |
|  | Inf | 13.844 | 2.3063 | 0.8895 | 0.4693 | 0.2915 | 0.1998 | 0.1464 | 0.1123 | 0.0892 |
|  | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

### 4.2.3 PID controller for **)**

| Constants | n=1 | n=2 | n=3 | n=4 | n=5 | n=6 | n=7 | n=8 | n=9 | n=10 |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
|  | Inf | 11.5554 | 5.5040 | 3.7567 | 2.9204 | 2.4284 | 2.1004 | 1.8676 | 1.6917 | 1.5513 |
|  | Inf | 30.7642 | 5.1251 | 1.9766 | 1.0429 | 0.6478 | 0.4438 | 0.3253 | 0.2497 | 0.1982 |
|  | 0.4092 | 1.0850 | 1.4777 | 1.7849 | 2.0444 | 2.2756 | 2.4847 | 2.6811 | 2.8652 | 3.0346 |

# 5. OBSERVATIONS & THEIR ANALYSIS

## 5.1 Inflection Points



These are the initial step responses of transfer functions from (As increases, the steady state value reduces gradually) . Further, we find the values and of their inflection points and plot the same with various multiplicities on the above graph (except at ). These responses for the original system are found to be an **.** This is a trait of lag systems.

**So, we apply the lag Z-N rules for the lag type systems.**

## 5.2 The anomalous case of

We observed that any inflection point could not be found in case of multiplicity

As it is obvious from the given transfer function that for unit step input, the output will be whose laplace inverse will give y(t) = . On differentiating it wrt time, we get y’(t) = and differentiating again, we deduce y”(t) = -1.5\*.

Now, we know that at y”(t) = 0 at inflection point but for transfer function with multiplicity k =1 we obtain y”(t) = -1.5\* which does not equate to ‘0’ for any finite possible value of time t.

Thus we conclude that there exists no inflection point for G(s) = .

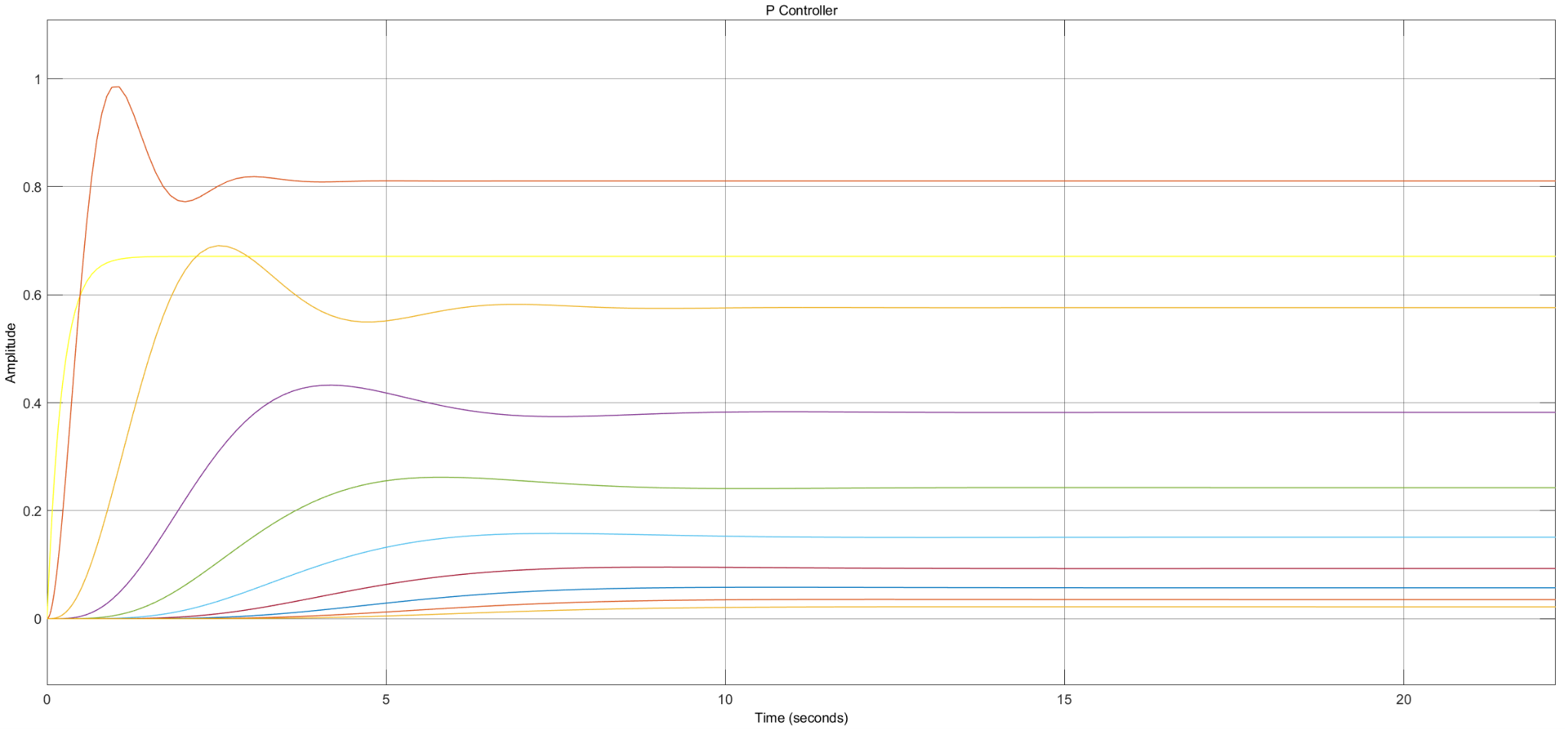
Further y’(t) = is a monotonic decreasing function which means the slope of the curve (output response) always keeps decreasing and hence the required tangent for finding the Z-N parameters is drawn at the starting point itself (where t = 0), but this lends us with the value of parameter L = 0, which inturn signifies that the gain parameter should attain an infinite value, which is not realisable at all !!

So, we found the values via tune methods of matlab. And the values were as follows:

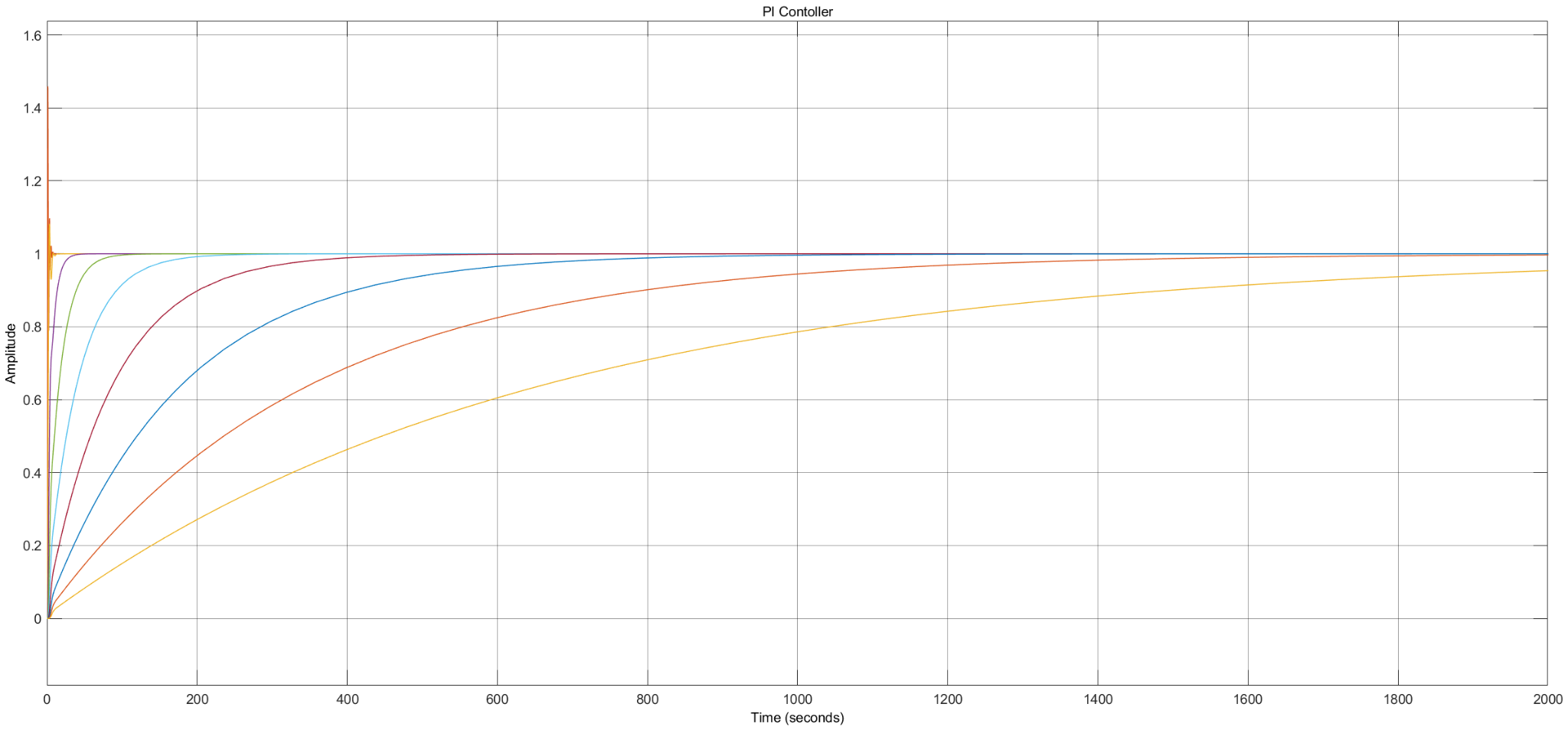
| Types of controller → | P controller | PI controller | PID controller |
| --- | --- | --- | --- |
|  | 3.06 | 1.56 | 2.15 |
|  | 0 | 7.04 | 5.84 |
|  | 0 | 0 | 0 |

## 5.3 Dynamic responses of CLTF curves and Performance Measures

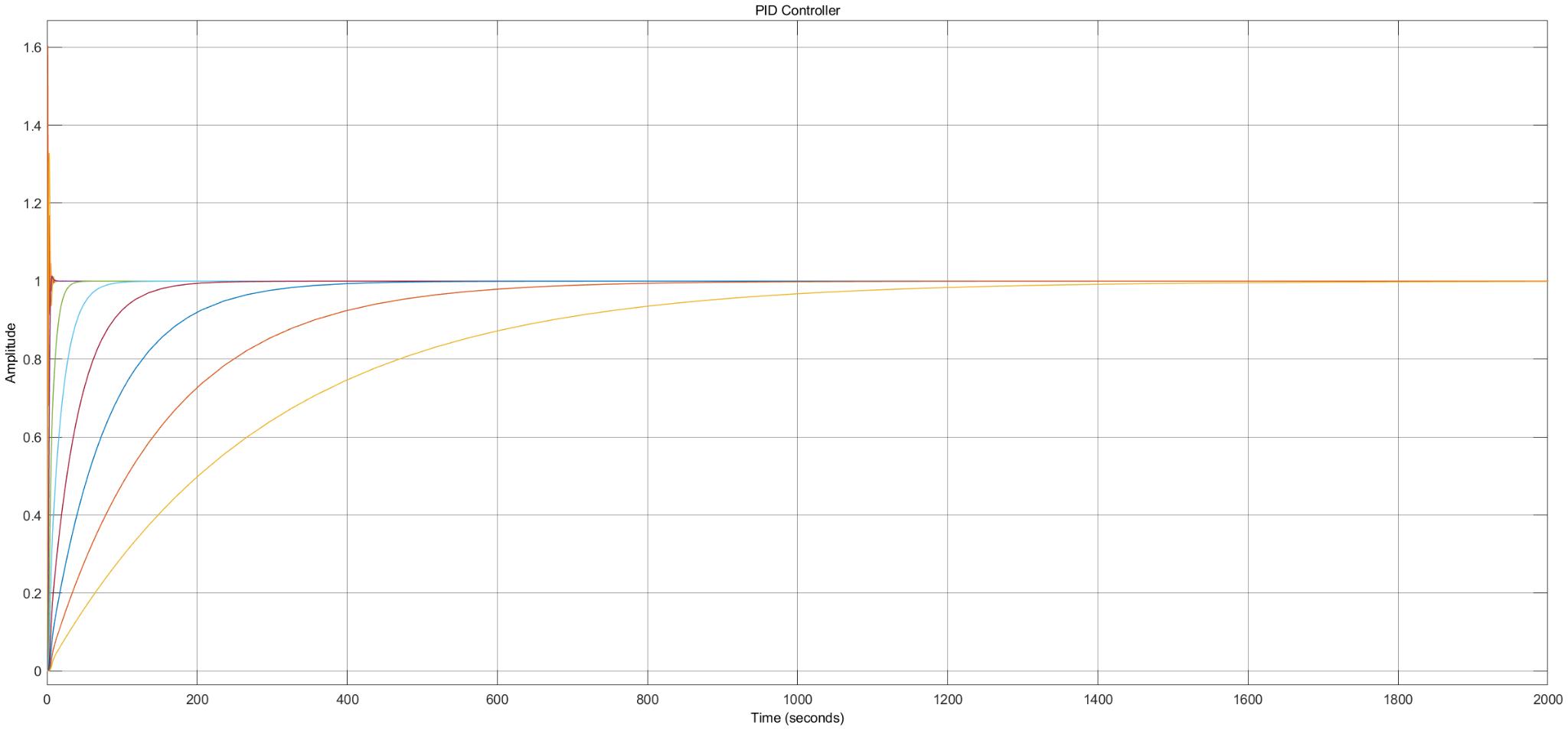
### 5.2.1 P controller



### 5.2.2 PI controller



### 5.2.3 PID controller



### 5.2.4 Performance Comparison Of P, PI and PID Controllers :

It should be noted that when multiplicity increases, the speed of decrease in rise time is quite fast for the PI controller as compared to the rest. The settling time decrement rate however is fastest for the P controller, followed by the PID and then the PI controller. The increase in overshoot is slight for the P controller but is drastic for others, and the steady state error is quite low for the PI and PID controllers as compared to the P controller.

## 5.3 Analysis of the effectiveness of the “ZN rules” for multiple poles systems

| **RISE TIME** | **SETTLING TIME** |
| --- | --- |
|  |  |
| **OVERSHOOT** | **STEADY STATE ERROR** |
|  |  |
| **STABILITY USING EIGENVALUES** | |
|  | |

| **Variation as multiplicity ↑** | **P Controller** | **PI Controller** | **PID Controller** |
| --- | --- | --- | --- |
| **Rise Time** | Decreases Gradually | Decreases Faster | Decreases |
| **Settling Time** | Settles very fast | Settles very slowly | Settles slowly |
| **Overshoot** | Increases Slightly | Increases Drastically | Increases Drastically |
| **Steady State Error** | Error increases | Very minute error | Very minute error |

## 5.4 Overall effectiveness of Z-N Rules:

1. P Controller:

* Not capable of stabilising higher order systems
* Works decent for first order systems
* To be used where the steady state value is not a factor
* Magnitude of eigenvalues is in between PI and PID. Oscillatory behaviour is reduced

1. PI Controller:

* Eliminates steady state error.
* Should not be used where the response needs to be achieved quickly(where low settling time is desired).
* It has a negative effect on speed of the response. PI controllers cannot determine the effect of forthcoming response.
* Magnitude of eigenvalues is lowest. Oscillatory behaviour is reduced.

1. PID Controller:

* Steady state error is minimised and it takes a long time to achieve the steady state.
* Stability is increased.
* A decrease in time constant increases the speed of settling time as compared to the case of PI controller
* Magnitude of eigenvalues is highest. Oscillatory behaviour is reduced.
* Proportional controller will help in minimising the rise time.
* With the help of an additional integrator the steady state error is reduced to almost zero. It will also increase the time to achieve steady state.
* Using the derivative controller we will be able to maximise the eigenvalues of the closed loop system and hence increasing the overall stability. It will also reduce the overshoot and improvise the transient response of the system.

**5.5 Limitations of Z-N Rules:**

* The required parameters for the Z-N test cannot be found for some abrupt situations like in this experiment only, for we could not find a desirable inflection point and hence the tangent could be drawn only at (except the steady state asymptote) , which led to the value of and hence non realisable and we could not use the Z-N method here.
* The steady state response is achieved after a long time, so the usage of these rules where we have to make a dead-time dominant process is not satisfactory.

# 6. CONCLUSION

* The P, PI and PID controllers of different multiplicities using the Ziegler-Nichols rules were designed using simulink.
* The dynamic step responses for the controlled systems were plotted and analysed. The trends in performance measures were also taken into account.
* The effectiveness of the Ziegler-Nichols rules was also discussed in context to different multiplicities of the system poles.
* The limitations of the Ziegler-Nichols test were also summarised.

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# 7. MATLAB SCRIPT

